

Arquitetura de Computadores

PVP 6 – Capítulo 5

Circuitos Aritméticos: Inteiros

José Coelho,
Gracinda Carvalho 2023



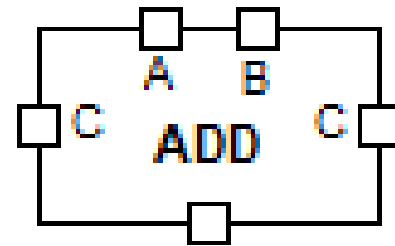
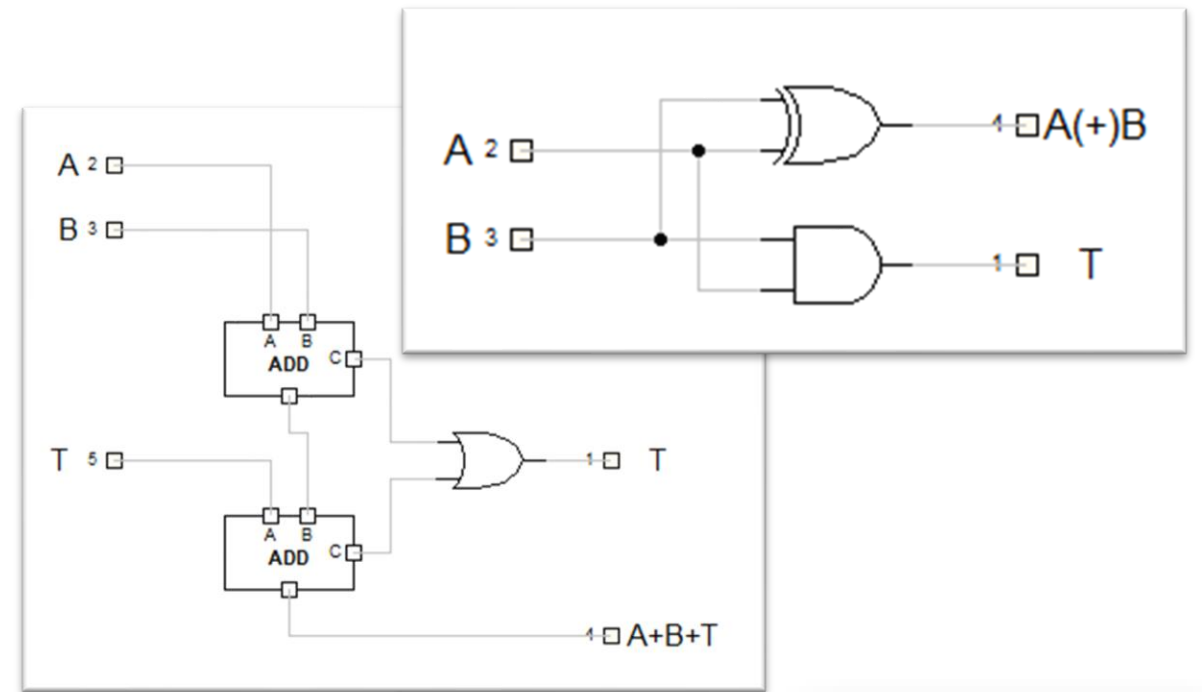
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Circuito Somador 1b

- Funcionalidade:
 - Somar 1 bit
 - Gerar transporte / somar transporte
- Iterativo:
 - Sinal de transporte
- Tabela de verdade
- Expressões lógicas
- Testes

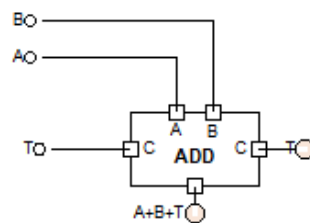


A	B	T	A+B+T	T
0	0	0	0	0
0	1	0	1	0
1	0	0	1	0
1	1	0	0	1
0	0	1	1	0
0	1	1	0	1
1	0	1	0	1
1	1	1	1	1

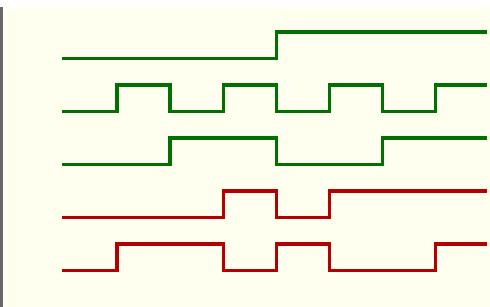
A	B	A+B	T
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$A + B = A \oplus B;$$

$$T = AB$$

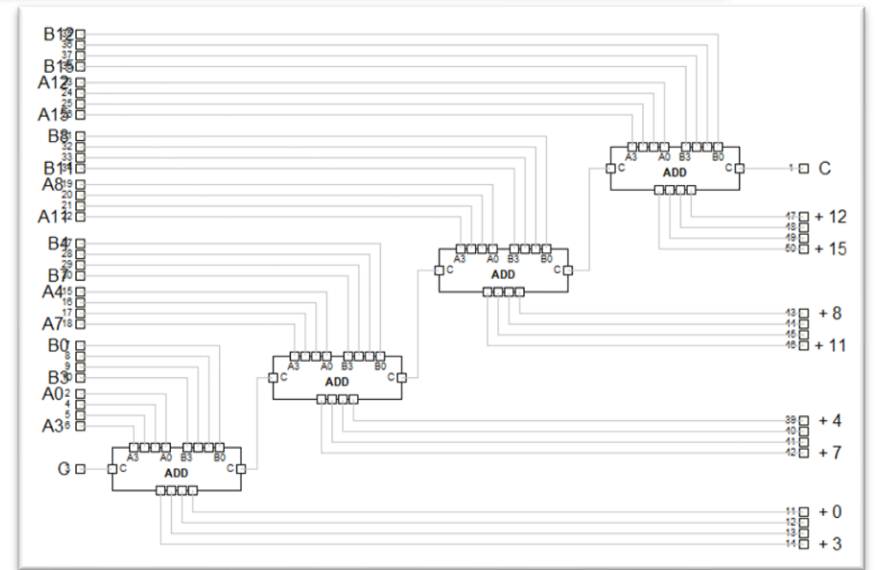
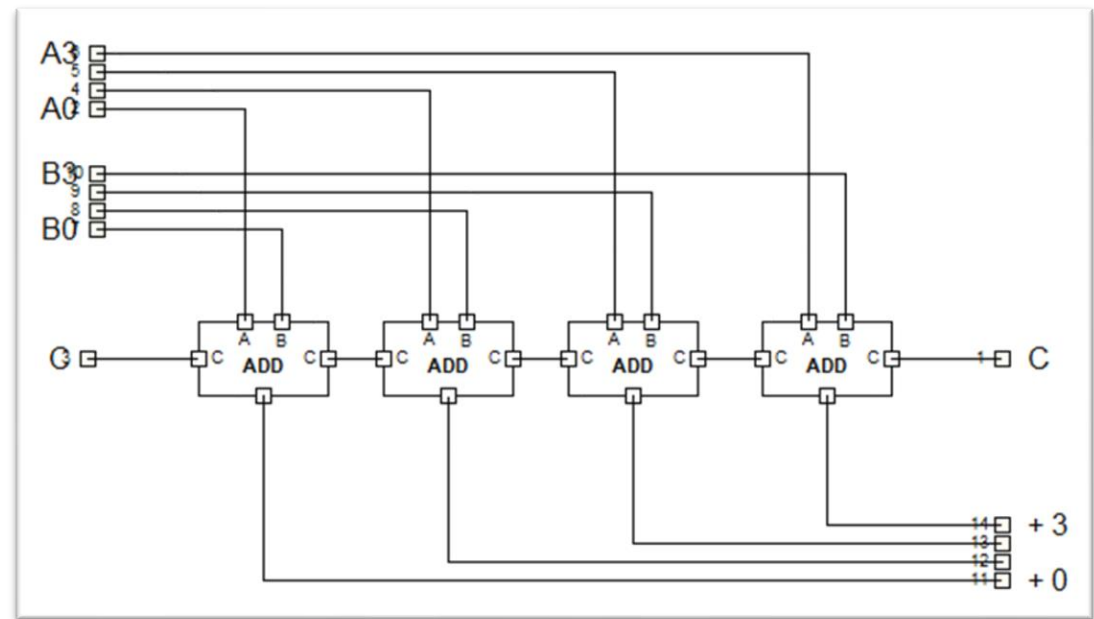
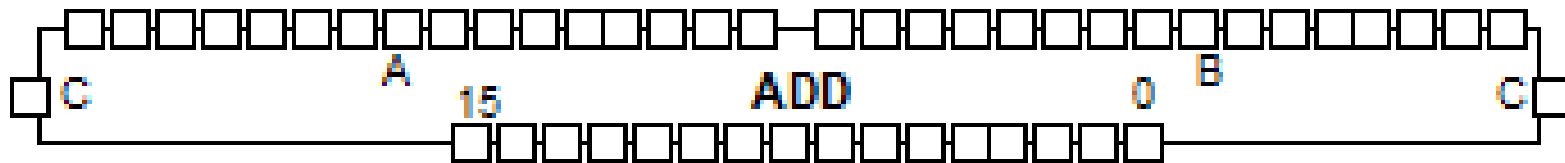
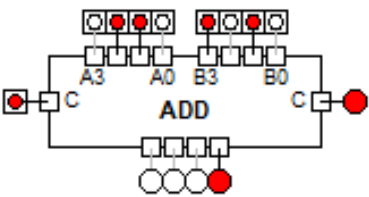
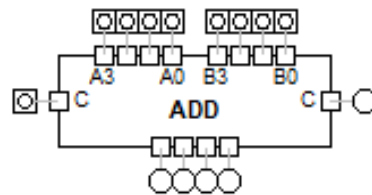
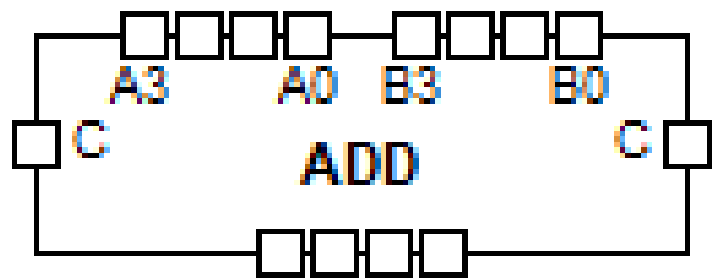


T
A
B
T
A+B+T



Somador 4b / 16b

- Reutilização: ADD 1b



Números com Sinal

- Possibilidades:
 - Módulo e sinal
 - Complemento para 2: $2^n - x$
 - Complementar todos os bits
 - Somar 1
- Alteração de número de bits
 - Módulo e sinal
 - Complemento para 2

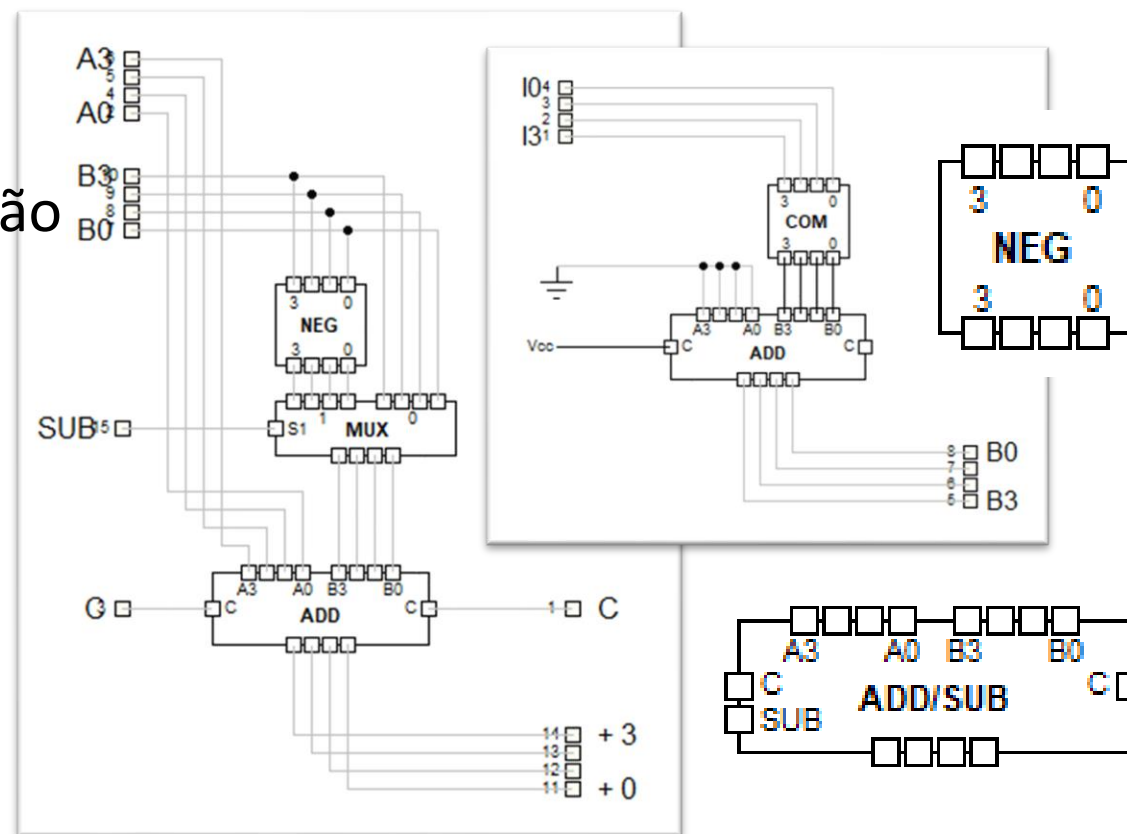
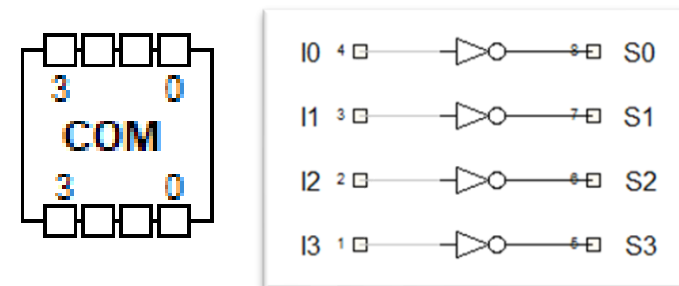
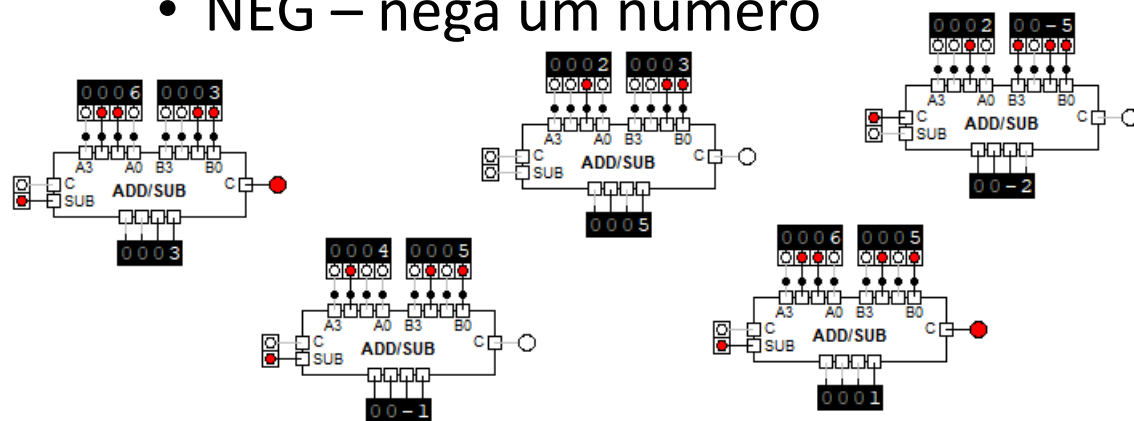
7	6	5	4	3	2	1	0	
Sinal	Bits com o módulo do número							Número
0	0	0	0	0	1	0	1	5
1	0	0	0	0	1	0	1	-5
0	0	0	0	0	1	1	0	6
1	0	0	0	0	1	1	0	-6

3	2	1	0	
Sinal	Módulo			Número
0	1	0	1	5
1	1	0	1	-5
0	1	1	0	6
1	1	1	0	-6

7	6	5	4	3	2	1	0	Número
0	0	0	0	0	1	0	1	5
1	1	1	1	1	0	1	0	~ 5
1	1	1	1	1	0	1	1	-5
0	0	0	0	0	1	1	0	6
1	1	1	1	1	0	0	1	~ 6
1	1	1	1	1	0	1	0	-6

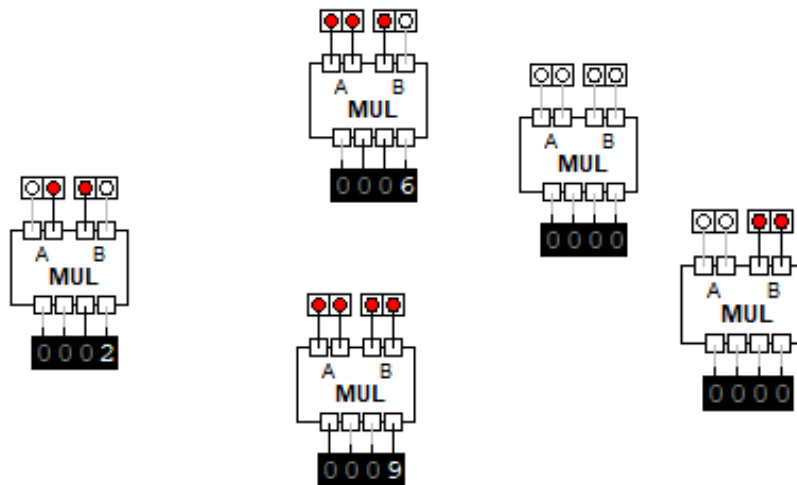
Somador/subtractor 4b

- Funcionalidade:
 - Somar ou subtrair dois números
- Metodologia:
 - Negar um dos números se for subtração
- Módulos:
 - COM – complementa todos os bits
 - NEG – nega um número

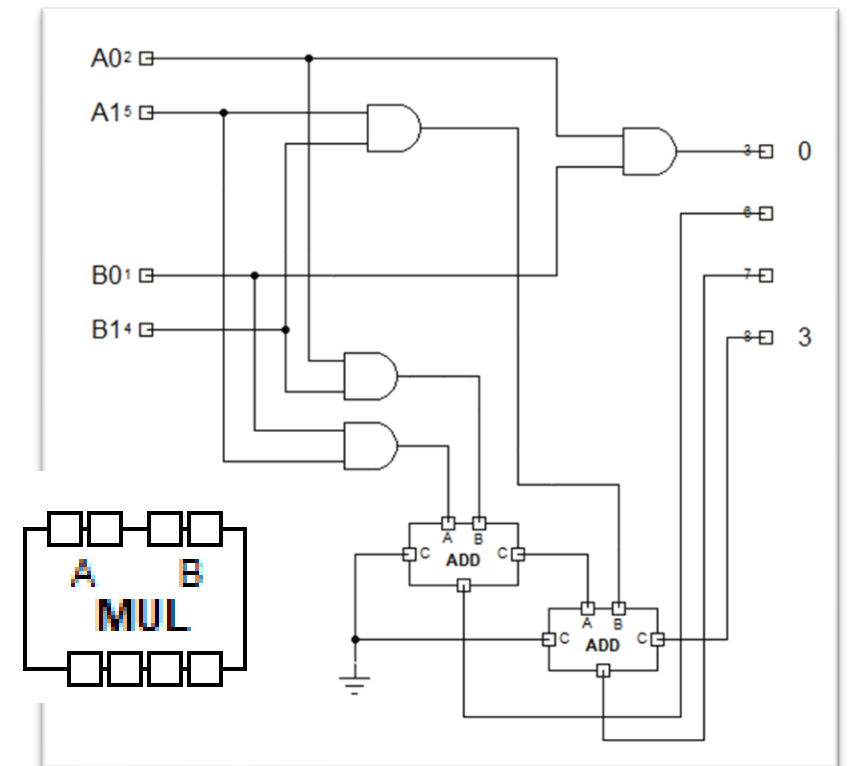


Multiplicação 2b


- Funcionalidade:
 - Multiplicar números de dois bits
- Metodologia:
 - Tirar partido do produto ser um AND

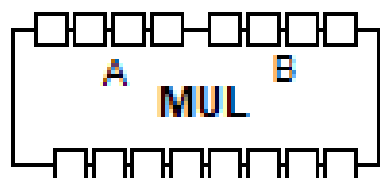
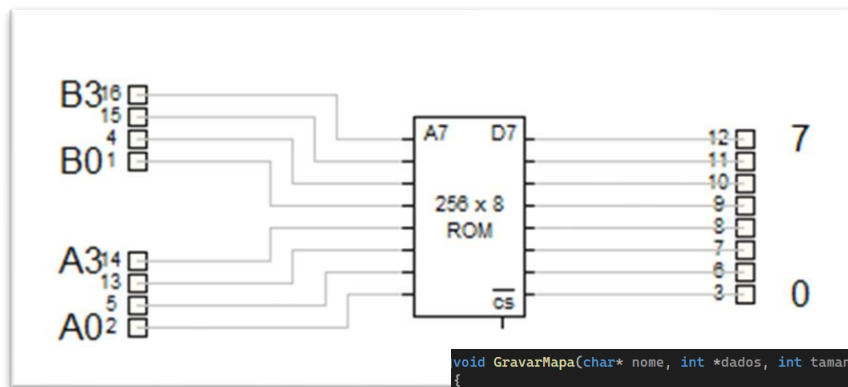
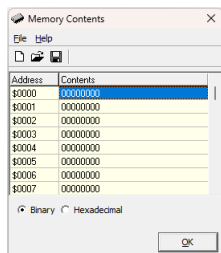
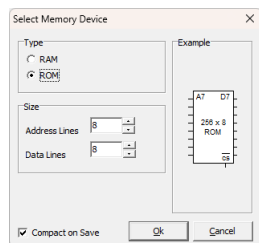
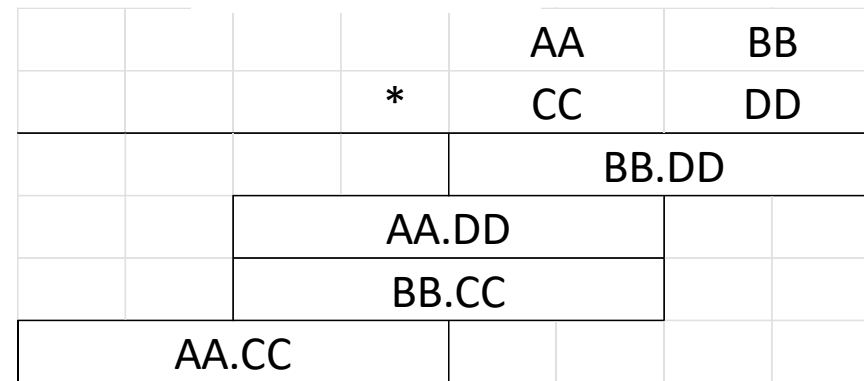
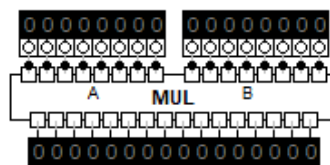
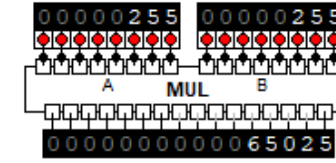
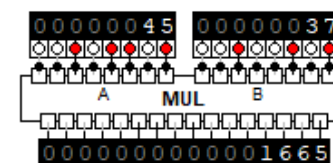
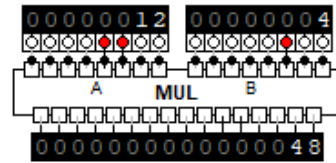


		A	B
	*	C	D
		AD	BD
	AC	BC	
T2	AC+T1	AD+BC	BD
	T2	T1	

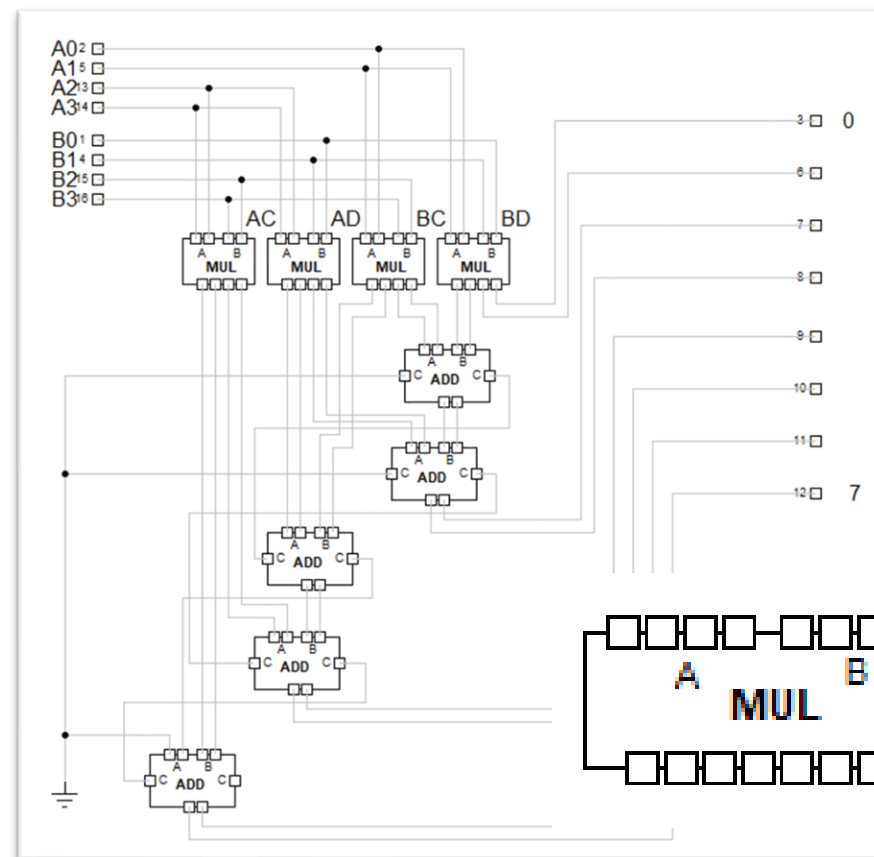


Multiplicador 4b / 8b

- Reutilização MUL 2b
- Utilizado para mais níveis
- Utilização de memória: 

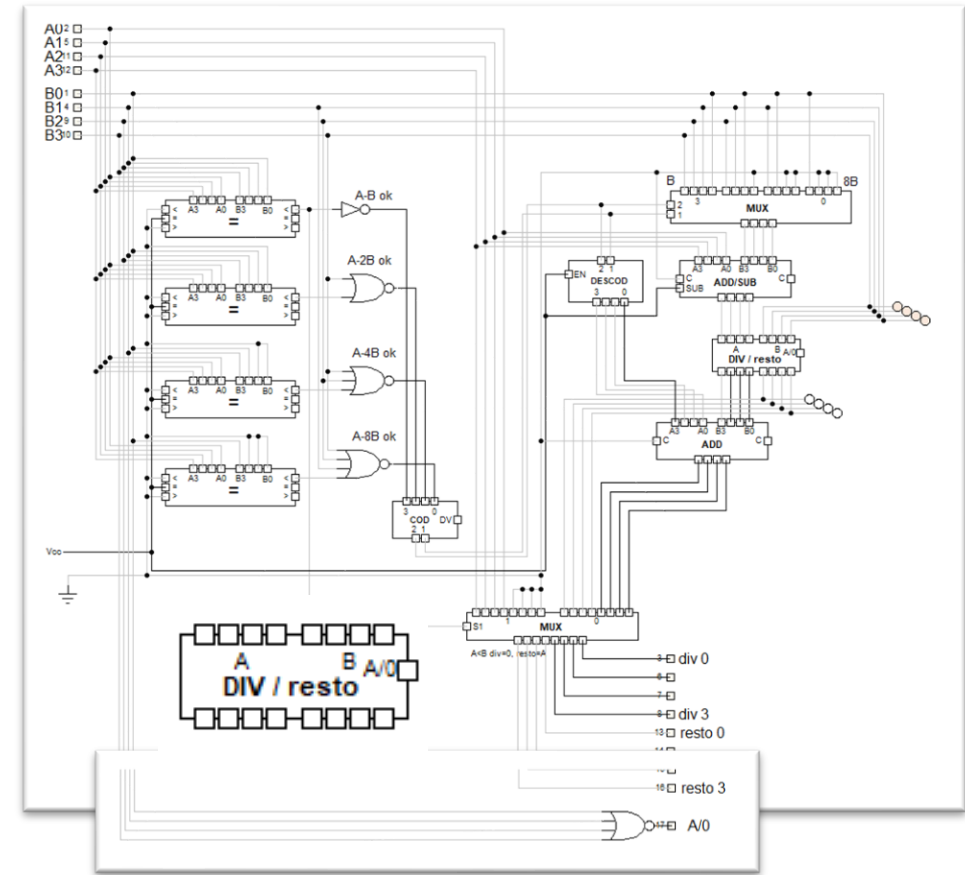
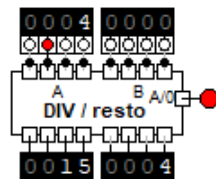
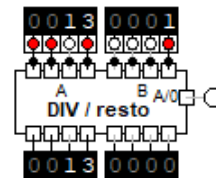
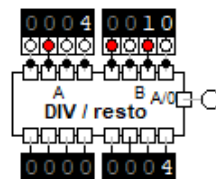
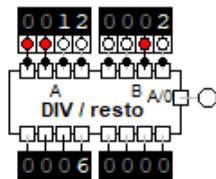
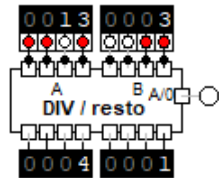


```
void GravarMapa(char* nome, int *dados, int tamanho)
{
    int cabecalho[] = {43981, 256};
    FILE* f = fopen(nome, "wb");
    if (f != NULL) {
        cabecalho[1] = tamanho;
        fwrite(cabecalho, sizeof(int), 2, f);
        fwrite(dados, sizeof(int), tamanho, f);
        fclose(f);
    }
}
```



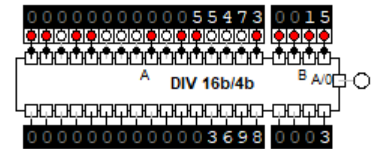
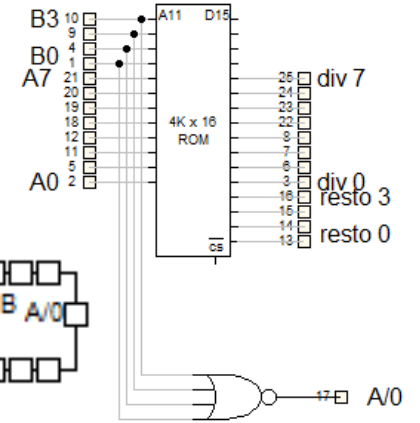
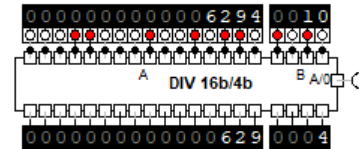
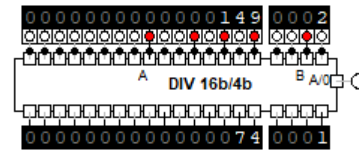
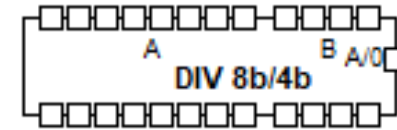
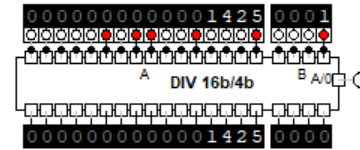
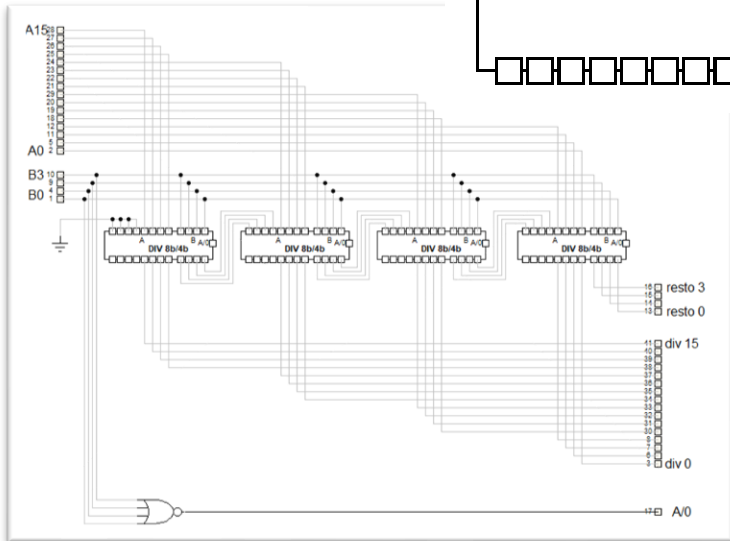
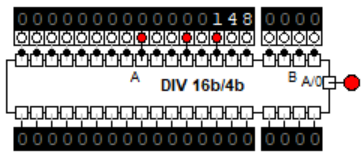
Divisores 4b

- Método de subtrações de potências de 2
 - $A \setminus B = \text{DIV}, \text{resto}$:
 - $A < B$? $\text{DIV} = 0, \text{resto} = A$
 - $A - 8B \geq 0$? $\text{DIV} = 8 + (A - 8B) \setminus B$
 - $A - 4B \geq 0$? $\text{DIV} = 4 + (A - 4B) \setminus B$
 - $A - 2B \geq 0$? $\text{DIV} = 2 + (A - 2B) \setminus B$
 - $\text{DIV} = 1 + (A - B) \setminus B$



Divisores 8b4b, 16b/4b

- Numerador com dobro dos bits
 - Metodologia: memória
- Permite estender o numerador



A	B	C	D	E			
r1(A/E)	B			d1(A/E)	d2(r1B/E)	d3(r2C/E)	d4(r3D/E)
	r2(r1B/E)	C					
		r3(r2C/E)	D				
			r4(r3D/E)				

Recursos utilizados

- Microsoft Power Point
- Clipchamp, voz de síntese Fernanda
- Vimeo
- G. Arroz, J. Monteiro, A. Oliveira (2020). Arquitectura de Computadores: dos Sistemas Digitais aos Microprocessadores (5ª edição). IST Press